

# **The Thermonuclear Runaway in SNe Ia** **(How to run away?)**

by **P. Hoefflich (Austin) & J. Stein (Jerusalem)**

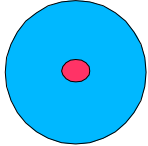
- **Introduction and open questions**
- **2-D calculations for the thermonuclear runaway**
- **Discussions and conclusions**

# Scenarios: What do we observe as a SNe Ia?

Thermonuclear explosion of a white dwarf

## 1) Hydrodynamical phase

- sudden release of about  $2E51$  erg by nuclear burning of a WD
- => object becomes unbound

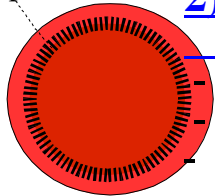


Duration of hydrodynamical phase: several sound crossing times

- sound velocity is about 5,000 to 10,000 km/sec
- radius of objects 1500 km (WD)
- => hydrodynamical time scale lasts seconds

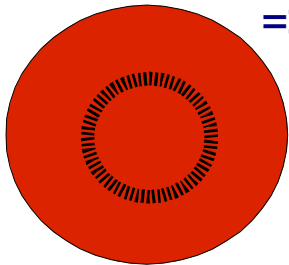
Photosphere

## 2) Subsequently: Phase of free expansion (homologous phase)



- We observe a rapidly expanding envelope as a result of the explosion !!!
- expansion velocities are 1000 to 20,000 km/sec
- we observe the light emitted from the photosphere
- With increasing time, the envelope becomes more and more transparent (due to geometrical dilution)

=> The time evolution of the emitted light  
allows to trace the radial density and chemical  
structure of the envelope !!!



## 1) Progenitors: Accreting White Dwarfs



**Start:** WD of 0.6 to 1.2 Mo

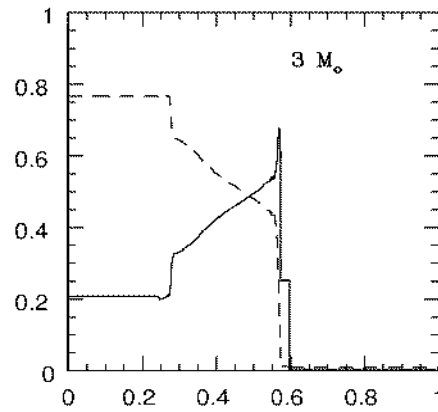
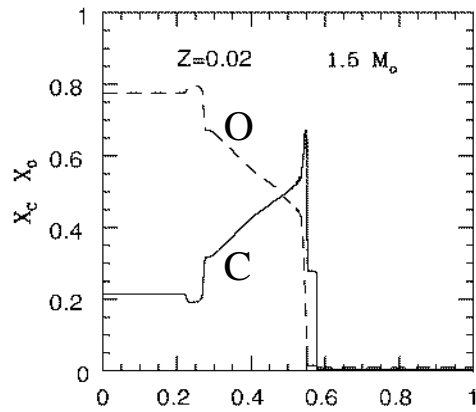
**Evolution:** Accretion of H, He or C/O rich material

**Explosion:** Ignition when nuclear time scales are shorter than hydrodyn. TS

## 2) Progenitors: Merging White Dwarfs

# Influence of the MS on the structure of the WD

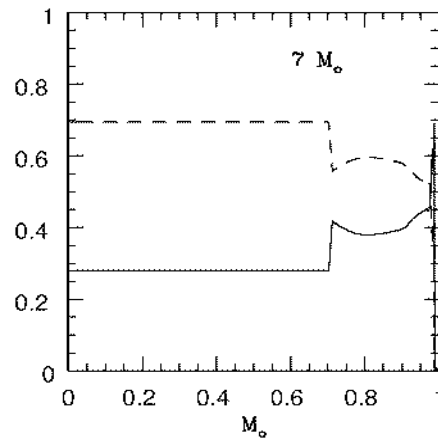
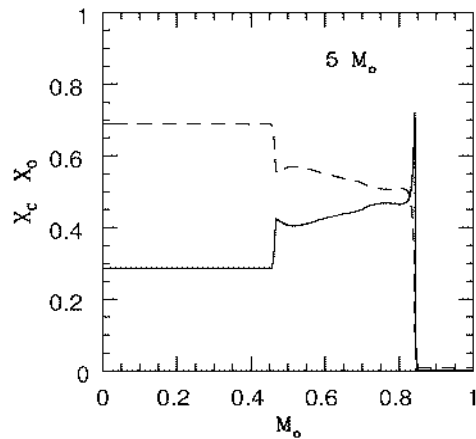
(Dominguez, Hoefflich, Straniero 2001, ApJ 557, 279)



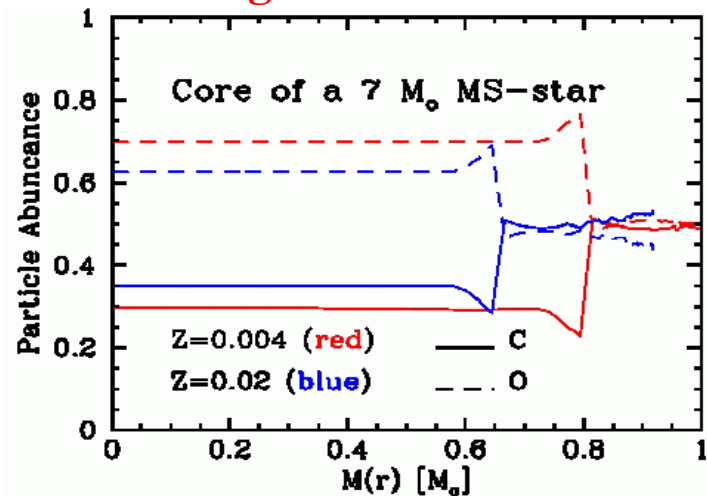
- Size of C-depleted core depends on central He burning during the stellar evolution

=>  $f(\text{MS})$

=> Explosion energy  $f(\text{MS})$

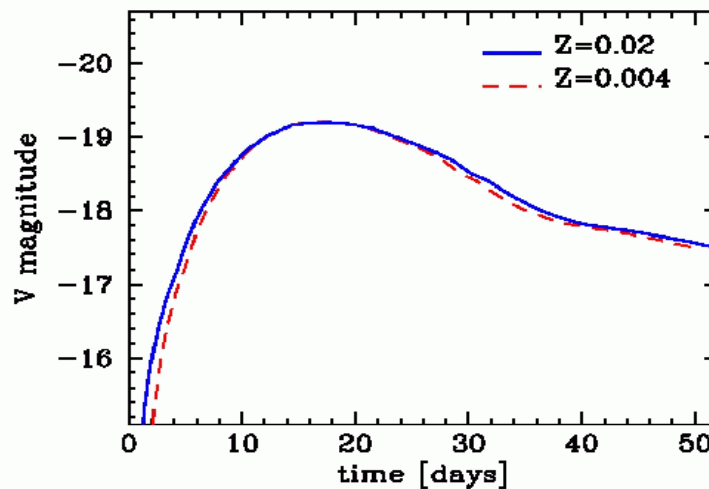
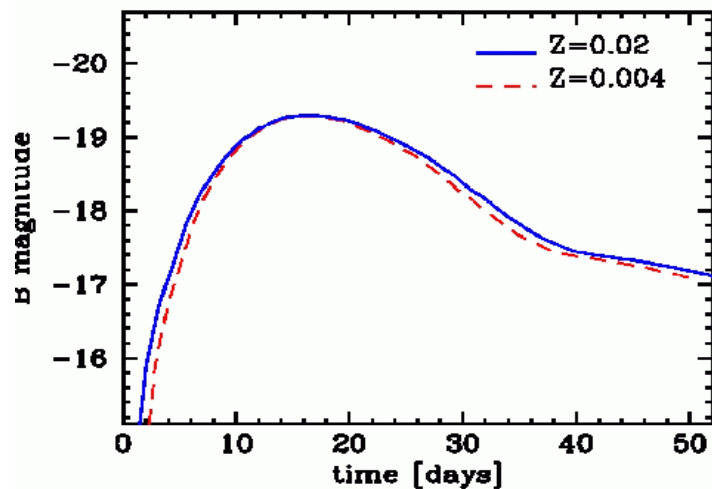


# Progenitor Structures, Metallicity Dependence and Consequences for the Light Curves of SNeIa (Hoeftlich, Nomoto, Umeda & Wheeler 2000, ApJ 528, 854)



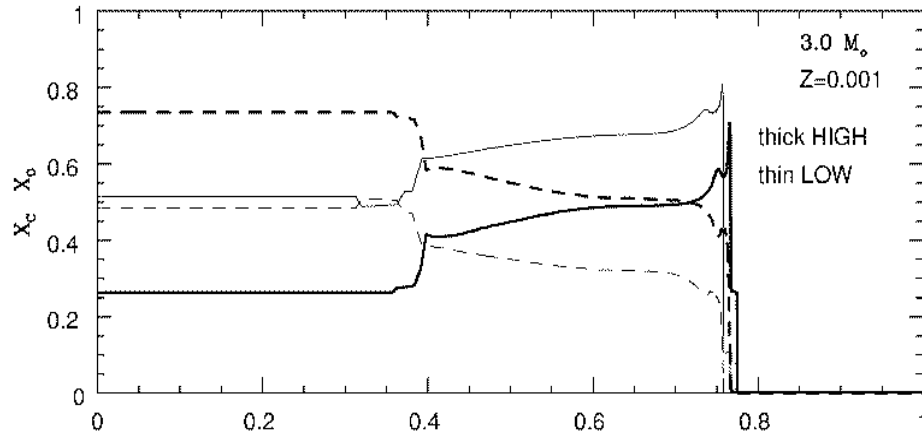
## EXPLOSION MODELS:

Mass = 1.38  $M_{\odot}$   
 $\rho_{\text{e}} = 2.5\text{E}9 \text{ g/ccm}$   
 $\rho_{\text{ur}} = 2.7\text{E}7 \text{ g/ccm}$   
 $\alpha = 0.02 \text{ c}_{\text{s}}$   
 $(\text{C/O})_{\text{M(CHH)}} = 0.38/0.43$   
  
 $M_{\text{v}} (\text{high-low } Z) = 0.02^{\text{m}}$   
 $M_{\text{v}}(\text{dM}_{10}) = 0.1^{\text{m}}$   
 $dt_{\text{v}} (\text{high-low } Z) = -1\text{d}$



# Influence of C12(alpha,gamma)O16 on the Structure

Dominguez, Hoeflich, Straniero 2001, ApJ 557, 279)

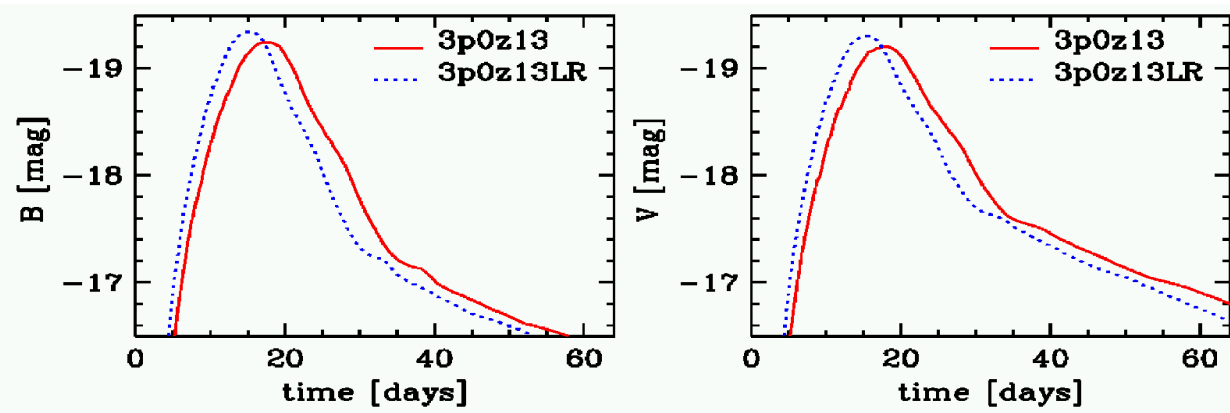


- Size of C-depleted core depends on the nuclear reaction rate (uncertainty fac. 5)

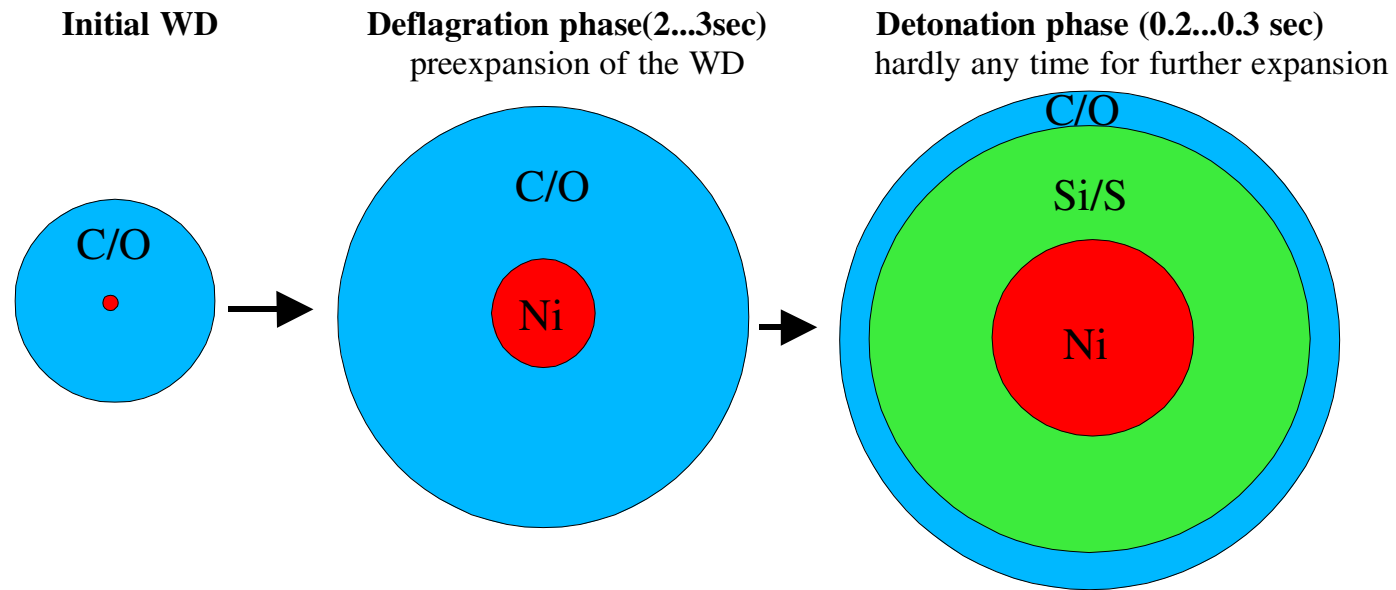
Caughlan et al.  
1985, At.Data Nuc. Tab. 32, 197

Caughlan & Fowler  
1988, At.Data Nucl. Tab 40, 283

Astrophysical Applications favor a high rate (e.g. Stellar evolution, LCs)



# Explosion Scenarios of White Dwarfs (Delayed Detonation)



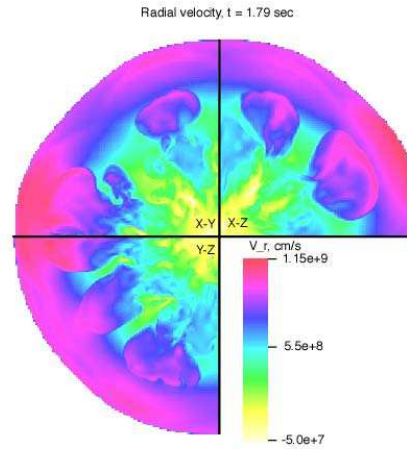
Deflagration: Energy transport by heat conduction over the front,  $v \ll v(\text{sound})$   
=> ignition of unburned fuel (C/O)

Detonation: ignition of unburned fuel by compression,  $v = v(\text{sound})$

■

# Propagation of the Deflagration Front (from Khokhlov, 2001, ApJ, in press)

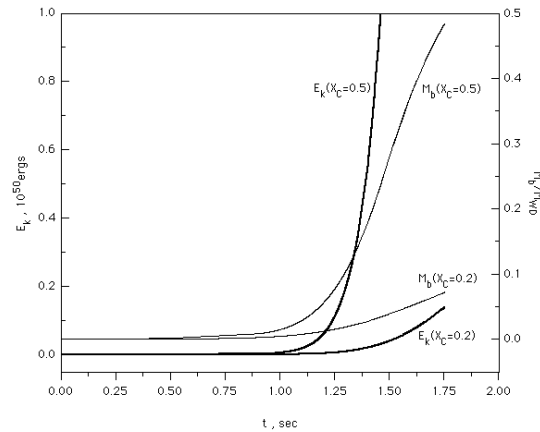
Burning of a WD at 2.5 sec (from ATP-2001 HK)



- Blobs mix into layers corresponding to about 8000 km/sec in the hom. ph.

## Some Remarks:

- pre-expansion depends on the amount of burning (-> does not depend on details of burning)
- expansion becomes spherical
- but inhomogenities in the abundances
- size and amount of burning depends on C/O





# Transition from Deflagration to Detonation

Possible mechanism:

1) Zeldovich mechanism: Mixing from burned and unburned material

- **Problem:** works only for low fluctuations in the background

2) Crossing shock waves (e.g. Livne 1997)

- **Problem:** Is the 'noise' sufficient or do we need some reflection at boundaries?

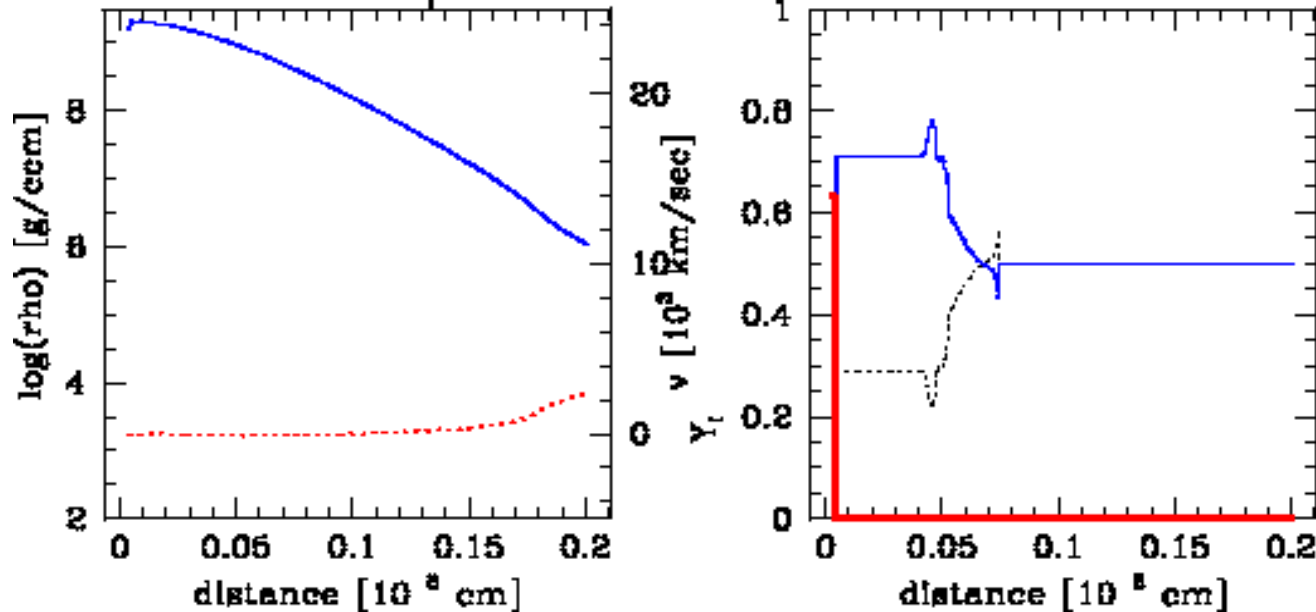
3) Shear flows at low densities (e.g. Livne/Aspen workshop)

- **Problem:** Does it work?

# Explosion of a delayed detonation model

- progenitor : 3Mo on MS with 1/30 of solar metallicity
- Properties of WD: a) Chandrasekhar mass b) central density  $2E9$  g/ccm
- Properties of deflagration front: a)  $v(\text{defl.})$  with  $C1=0.15$  b)  $\rho(\text{tr}) = 2E7$  g/ccm

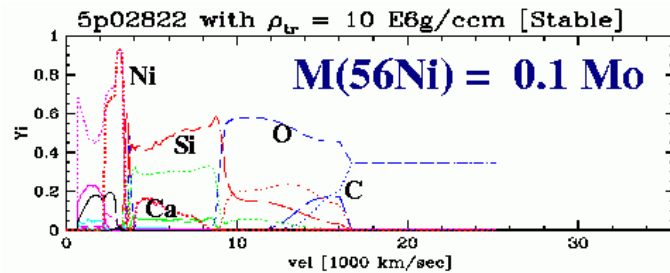
MODEL 3p01323 at 0.2 seconds



**red:** complete b. (Fe, Co, Ni) ; **green:** incomplete b. (Si, S, ...) ; **blue:** C and O

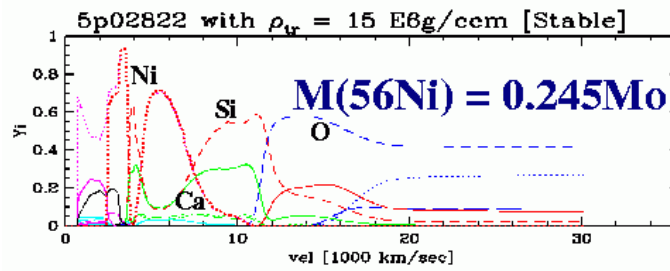
# Chemical Structures for Delayed-Detonation Models

## C/O-WD; $\rho(c)=2.E9$ g/ccm; $M(MS)=5M_{\odot}$



- start with slow deflagration front  
RT unstable  $\rightarrow$  acceleration

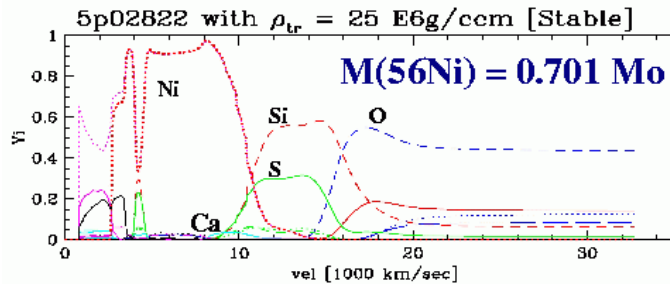
- Prompt transition to detonation



- Produces both normal bright and subluminal SN

- Avoids problem electron capture at the center.

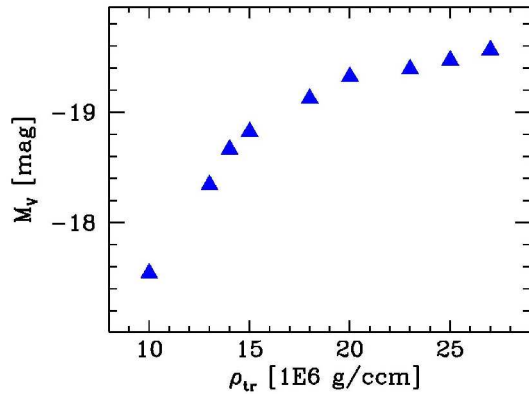
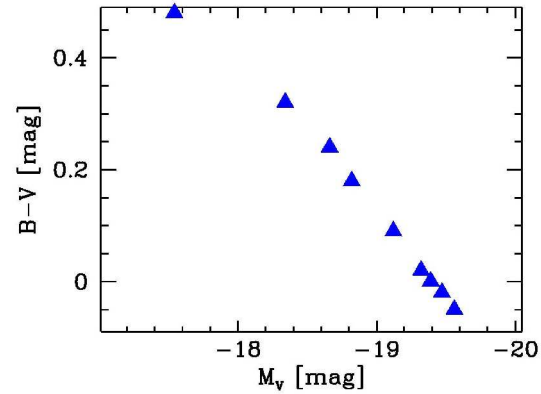
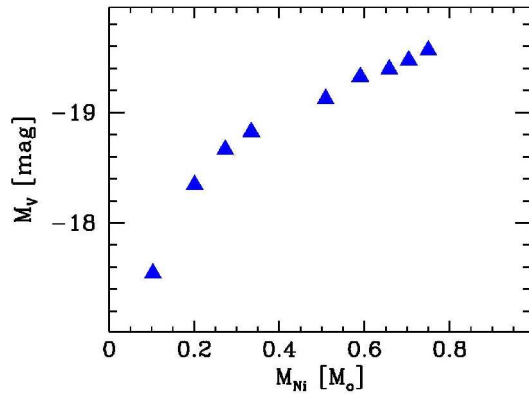
(with new rates + adaptive mesh-hydro.  
 $\Rightarrow \rho(c)$  may be up to  $3.5E9$ g/ccm)



(Fits well for a lot of S NeIa)

# Correlations for DD-Models

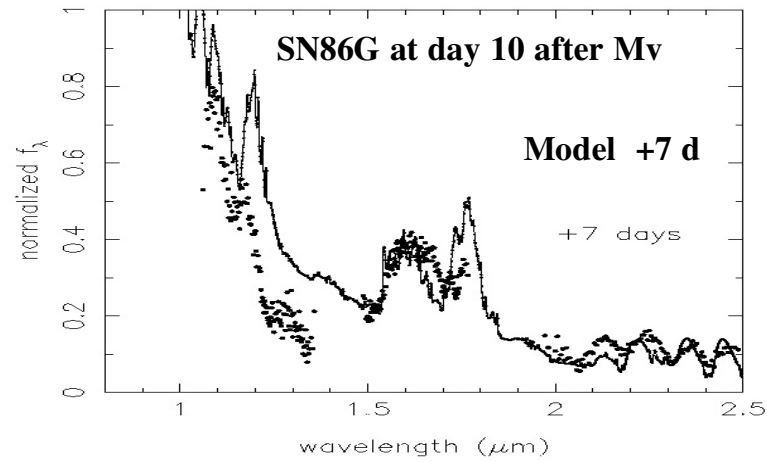
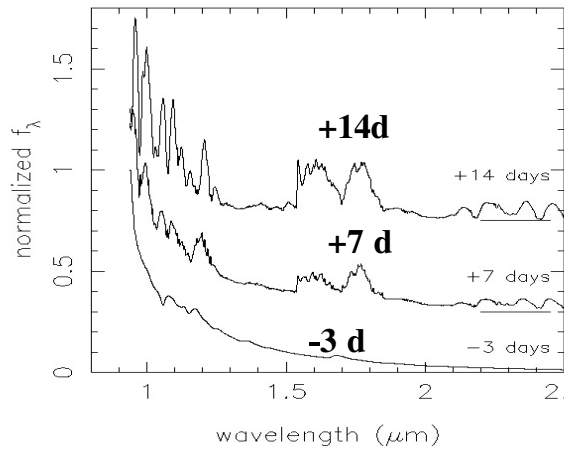
Example:  $\rho(c)=2.E9g/ccm$ ;  $M(MS)=5M_{\odot}$



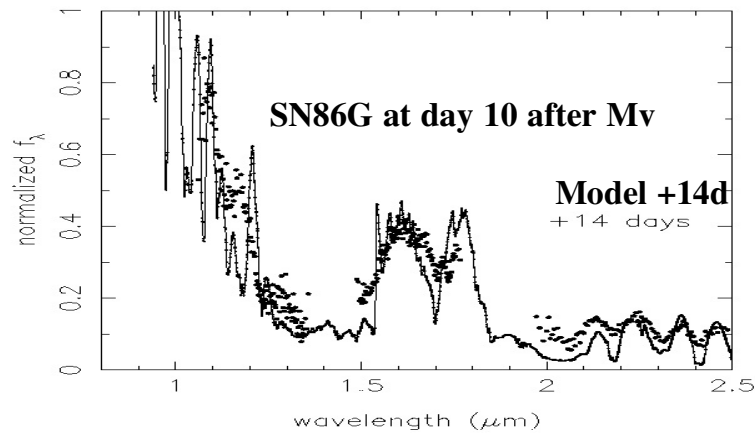
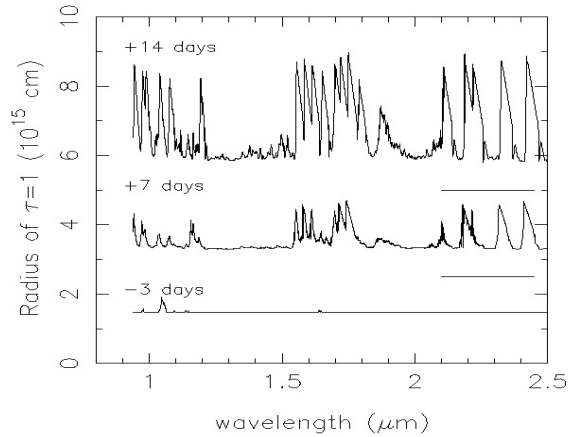
- $\rho(tr)$  determines  $M(Ni)$   
(See Hoefflich 1995)
- models are similar bright for a wide range of parameters !

# Post-maximum IR-Spectra of DD200 in Comparison with SN86G

Flux between 1 and 2.5  $\mu\text{m}$



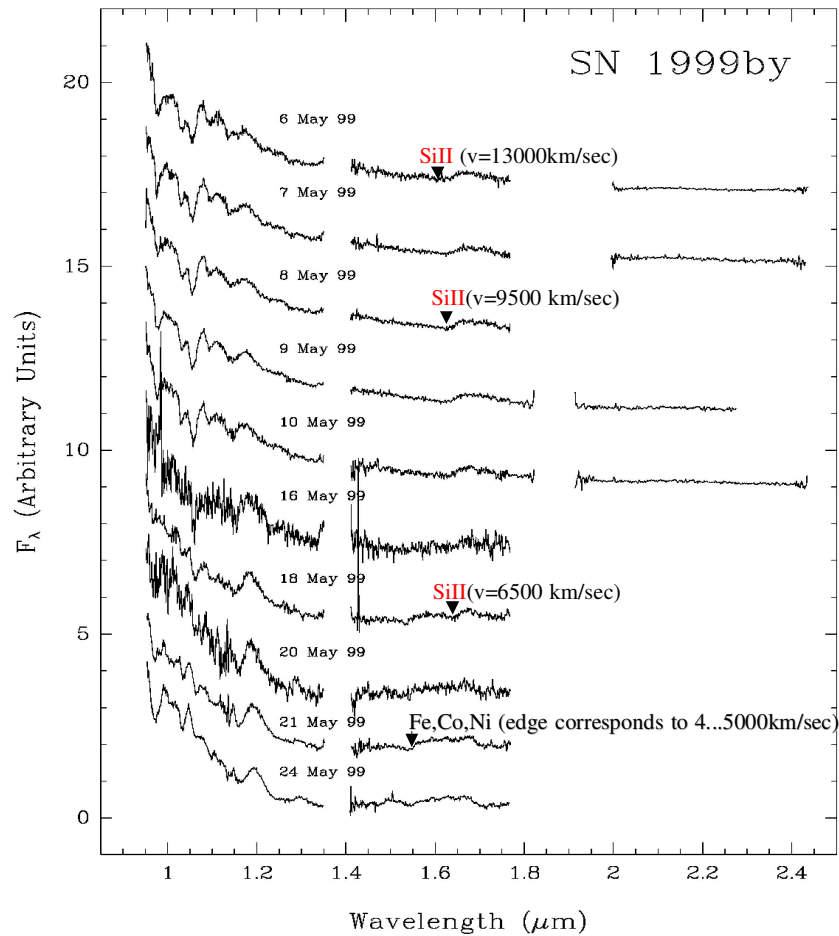
Radius between 1 and 2.5  $\mu\text{m}$



Observation of SN1986g by P. Meikle et al.

# IR-Spectra of the Subluminous SN1999by

Observation by C. Gerardy (PhD thesis)

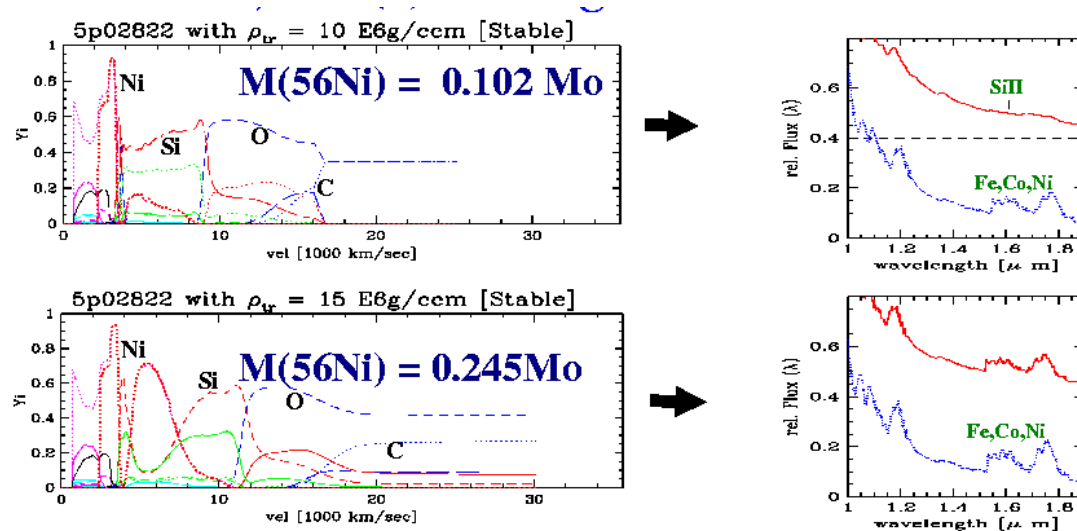


- M(V) on May 8

Rem: Quoted velocities are based  
on the Doppler shift of absorption  
minima  
(Uncertainty is about 2000 km/sec)

# Structures and IR Spectra for Subluminous DD-Models

C/O-WD;  $\rho_{\text{c}}=2.E9 \text{ g/ccm}$  IR-flux 1 & 2 weeks after M(V)

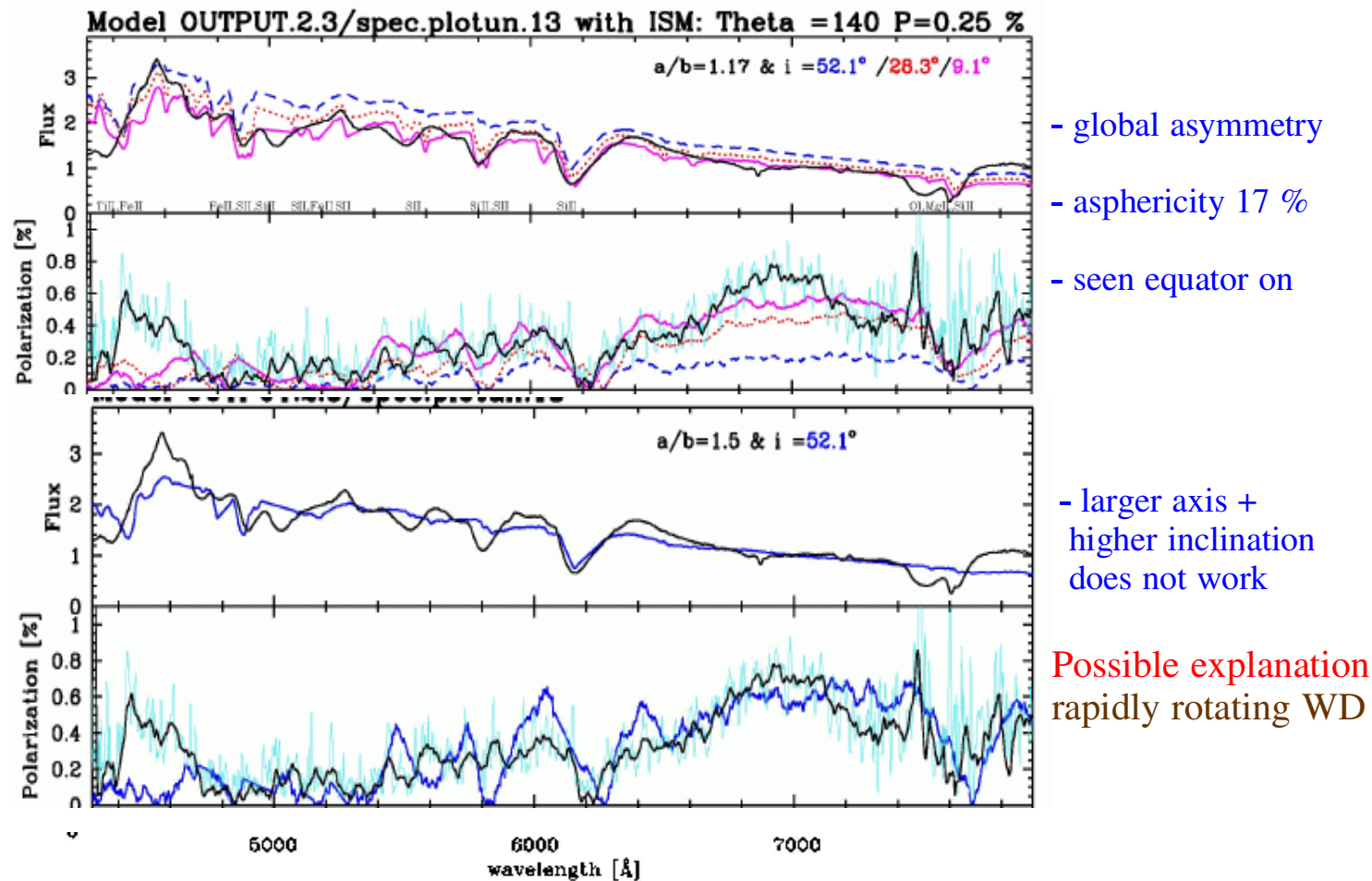


- Only very subluminous models are consistent with SN1999bu
- Layers up to 12-15000 km/sec must undergo explosive O-burning
- Strong mixing or extended Ni-tails are not allowed (PDD5 and PDD1c problems)
- Models shall not mix large blobs into the outer layers during deflagration!!!

Is this specific/the reason for subluminous SNeIa ???

# Polarization of the subluminous SN1999bu vs. prolate model

(PhD thesis of A. Howell & Howell, Hoeflich, Wang, Wheeler, ApJ, in press)





**=> The explosion is determined by the preconditioning of the WD**

- the propagation of the deflagration front depends on the C/O ratio
- the DD-transition may depend on
  - a) the C/O ratio
  - b) the location and jump in the chemical profiles of the WD
- Subluminous SNIa may be produced by rapid rotation of a WD

## **Questions**

- Does the chemical profile 'survives' on the way to the runaway?
- Does the thermonuclear runaway occur in multiple spots?
- Does we start off with a static WD?

# Models for the Progenitor Evolution

## A) Spherical accretion models

### Physics:

- implicit, quasi-static evolution in first order for the standard stellar structure equation (Hoeflich et al. 1998)
- energy transport by
  - a) conduction (Itoh et al. 1983)
  - b) convection in the mixing length theory
  - c) radiative diffusion including Kramer's and ff-opacities
- detailed nuclear network (35 nuclei up to 24Mg)
- detailed equation of state (Nomoto et al. 1982)
- thermal pulsed of H/He burning are treated by Sato (1980)

### Recipe:

- Take the core of a star ( $M < 8M_{\odot}$ ) at the end of He burning
- Accrete H, He or C/O material with a given rate
- Follow the evolution over 1E6 to 1E8 years up to the explosion

## B) Follow the last few hours till runaway in multi-D

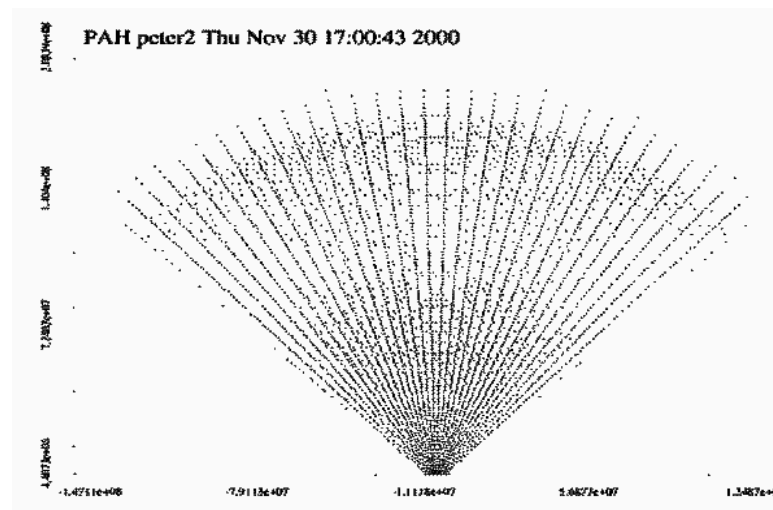
### Physics:

- implicit, 2-D hydrodynamic equations in first order in time
- interpolated energy for nuclear burning calibrated by detailed network
- detailed equation of state

### Recipe:

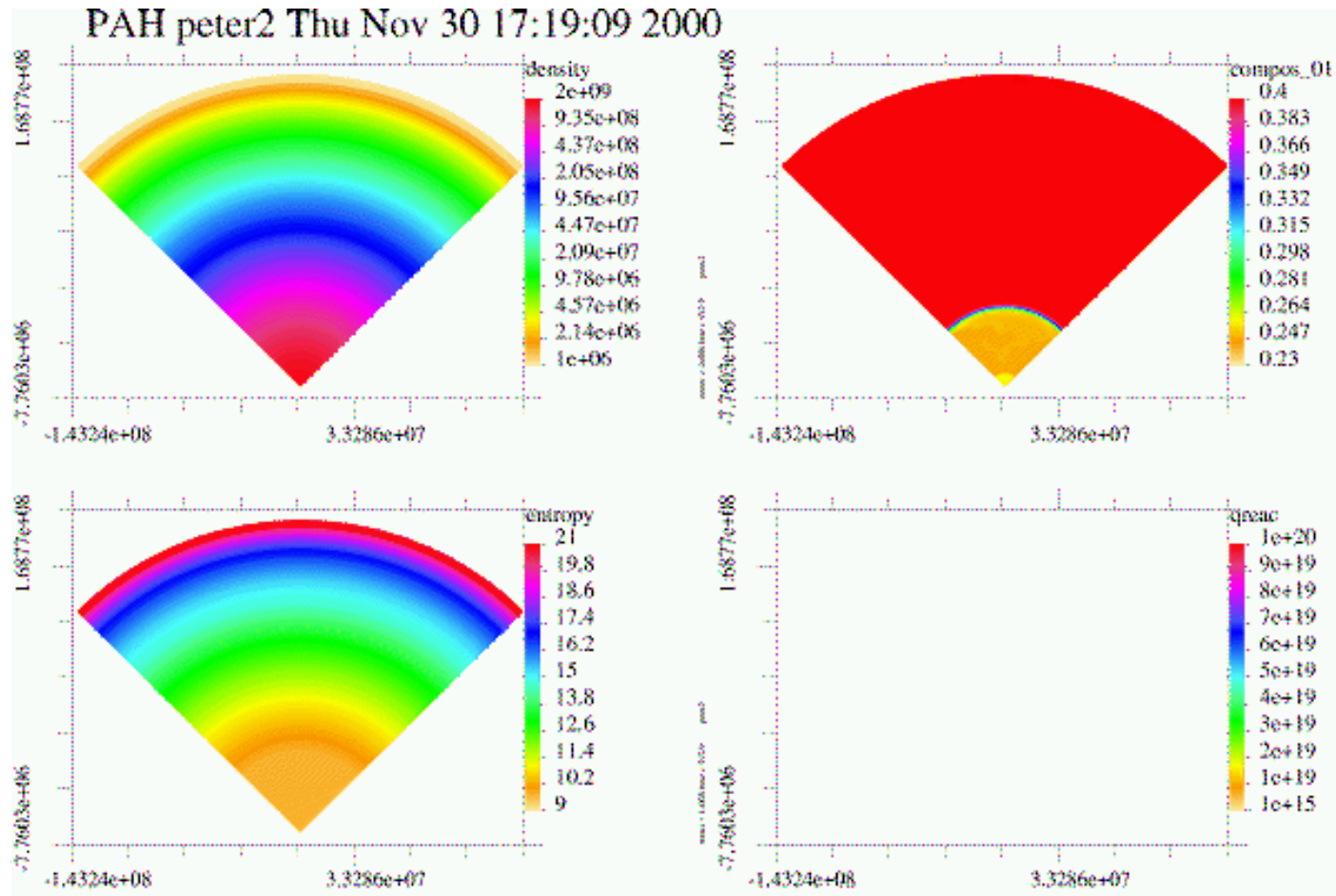
- Remap 1-D structure at about 5 hours before runaway and follow the evolution

Domain:  $2.08E8\text{cm}$   
Logarithm grid in r  
Grid(r/theta): (191/31)



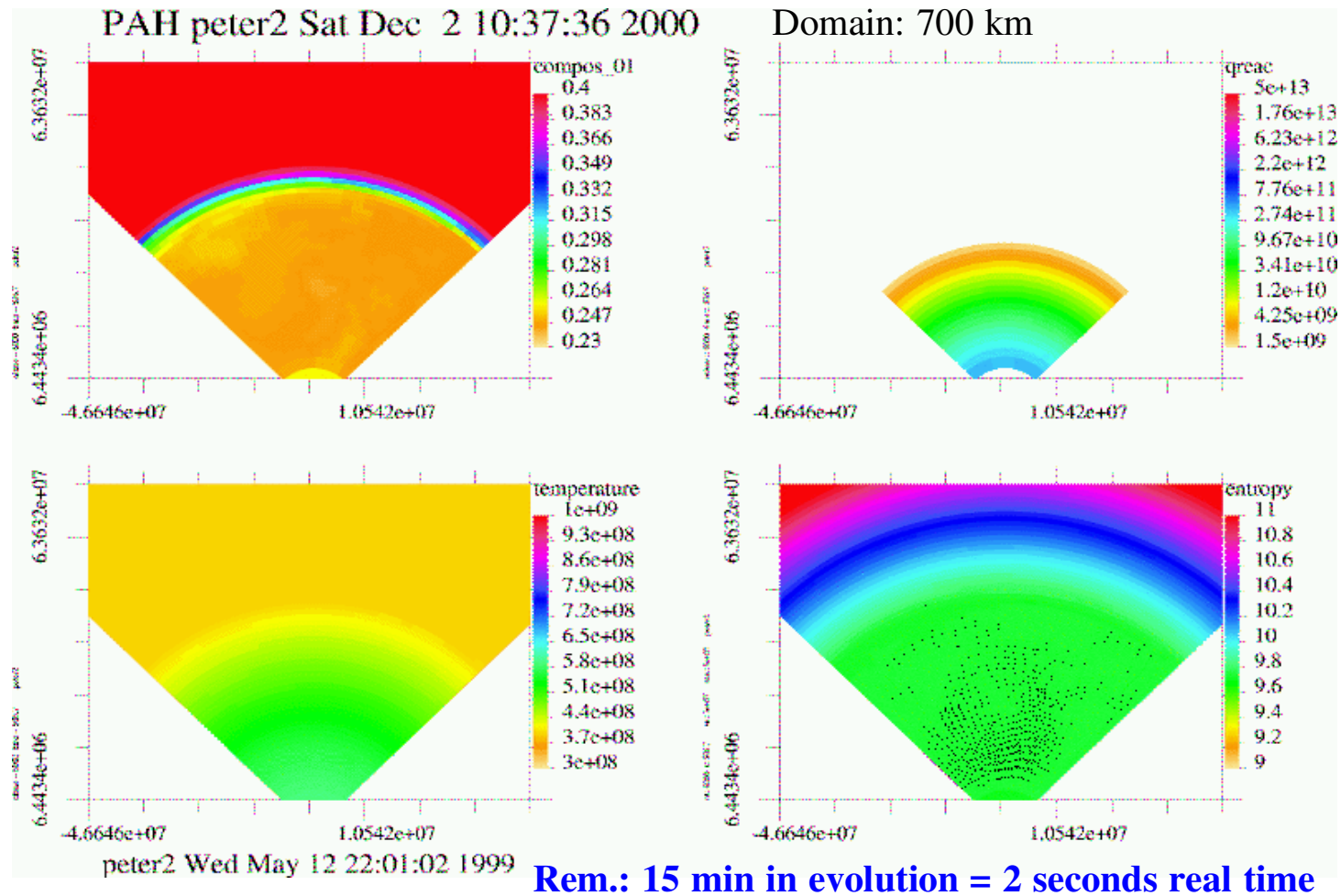
# The thermonuclear runaway of a WD (Hoeftlich&Stein,2002,ApJ, in press)

Initial structure 2 hours before runaway



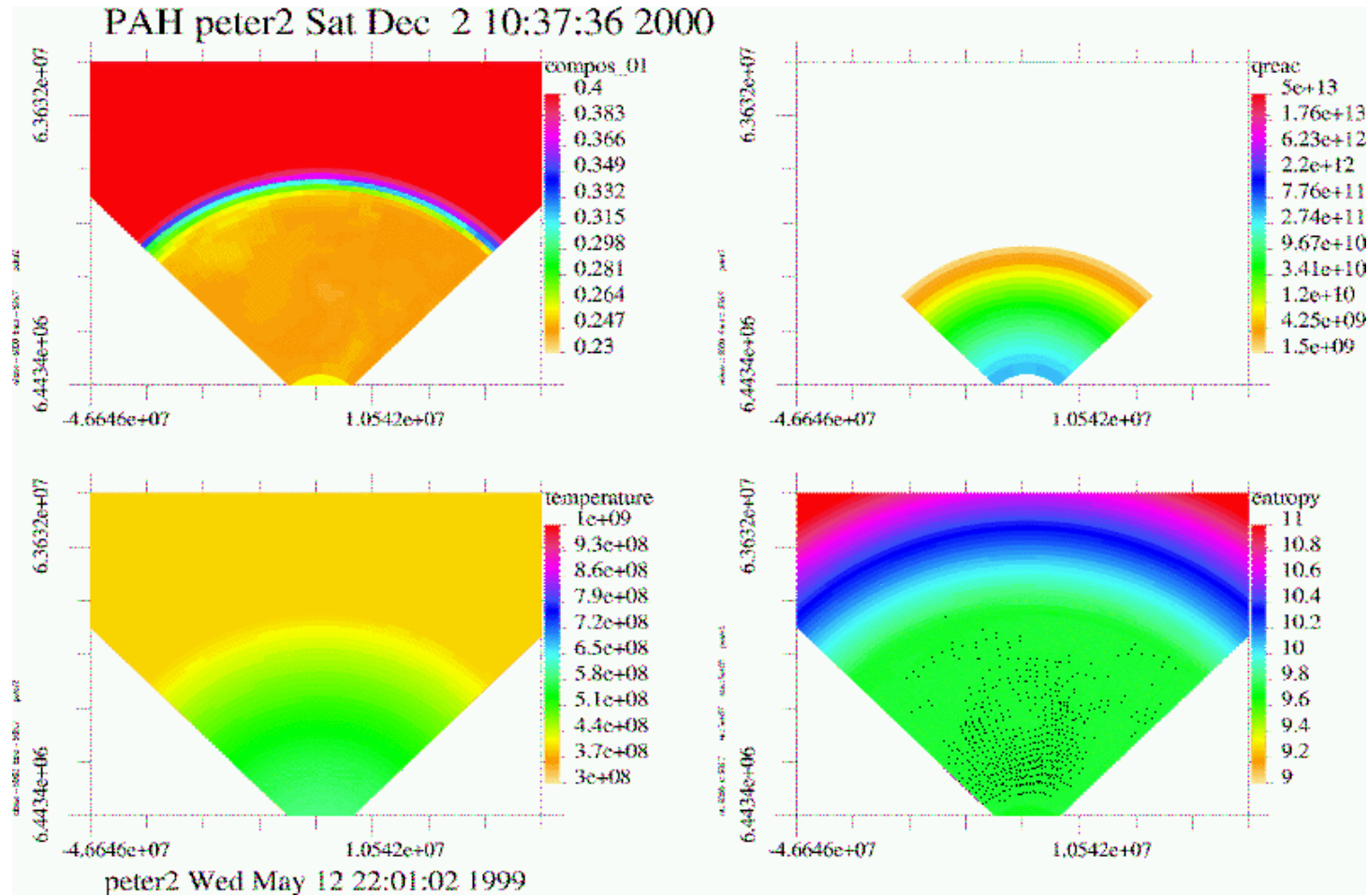
# The thermonuclear runaway of a WD

Time evolution from -3 to -0.5 hours with  $\Delta t=0.5h$  and at -900, -450, -225, -1 sec



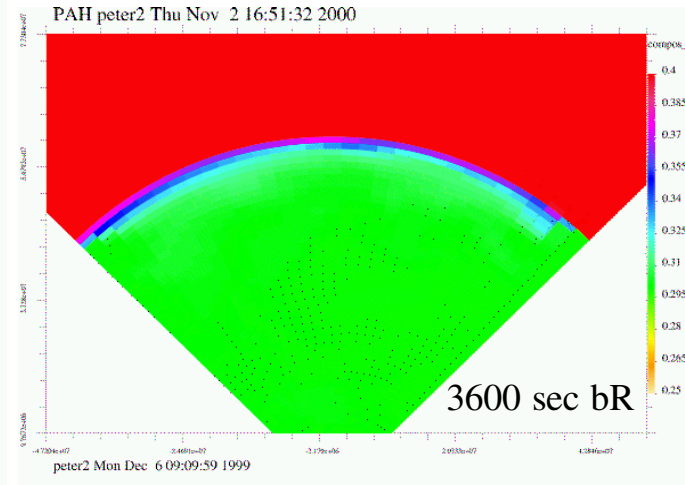
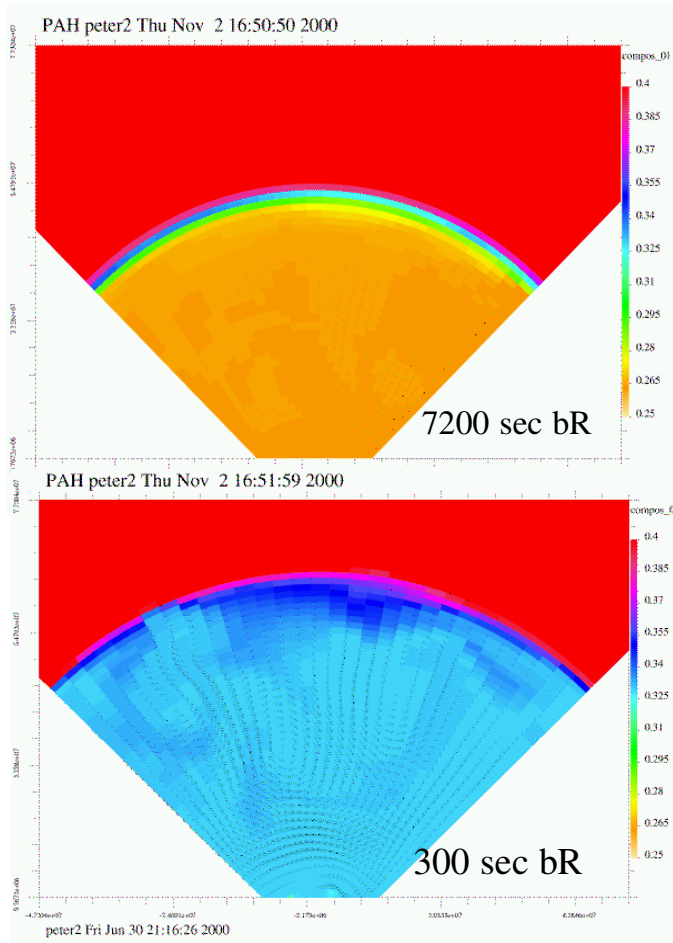
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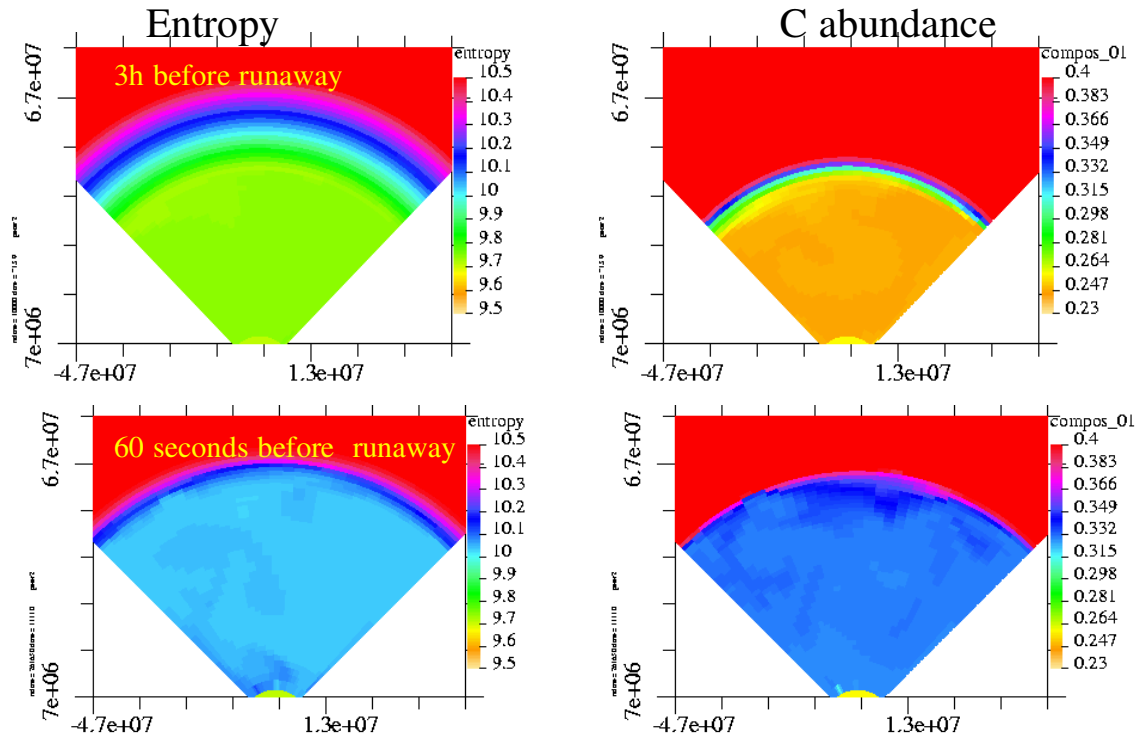
# The thermonuclear runaway of a WD

a) Change of C/O and velocity in the WD ( $M_{\text{ch}}$ ,  $M(MS)=3M_{\odot}$ )



Change of the CO before runaway  
velocities (longest = 100 km/sec)

# How to estimate the final C abundance in the center ?



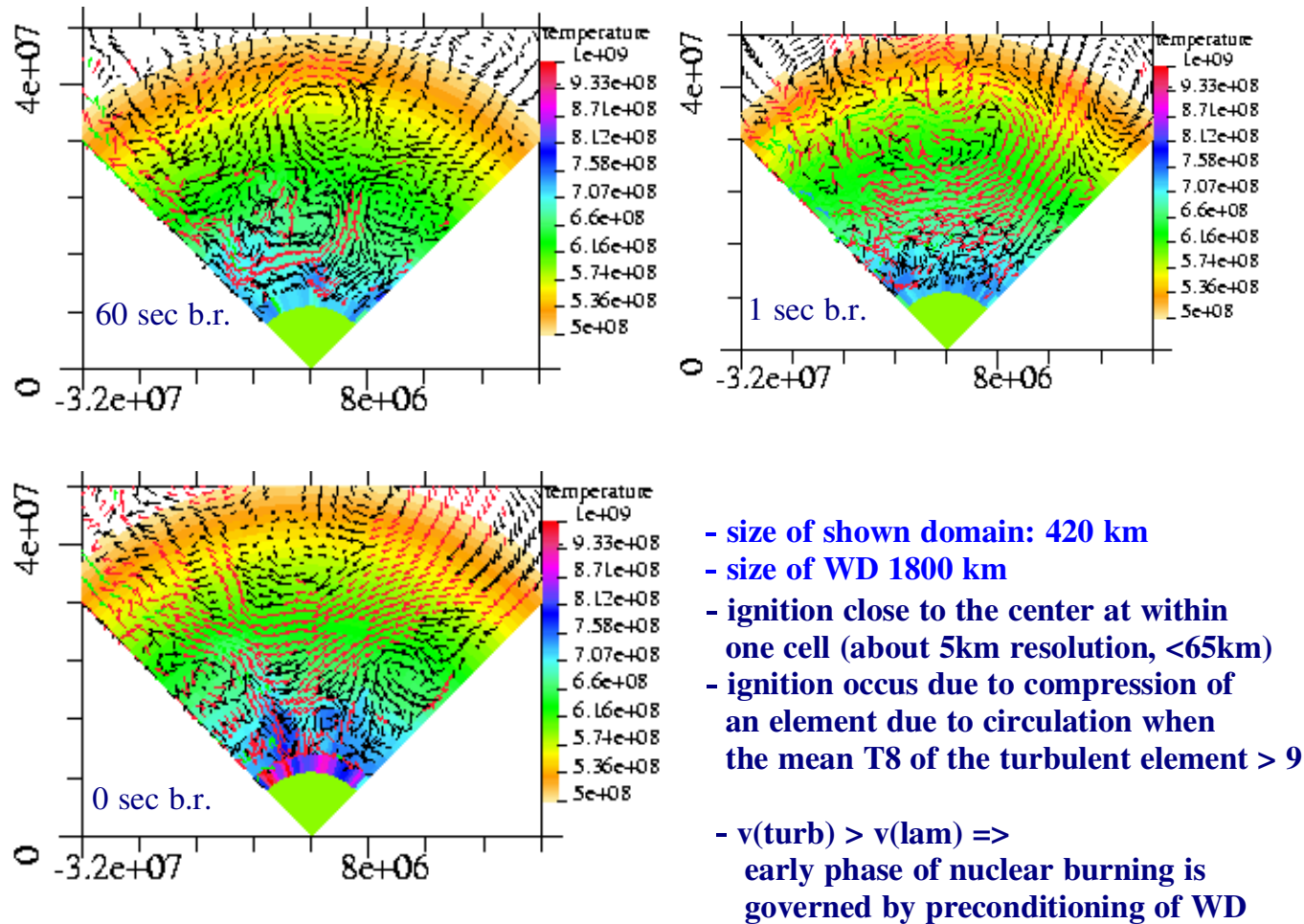
- entropy is almost constant in the convective center
  - runaway occurs at an mean entropy is about 10.1 (up from about 9.7)
  - C originates from to mixing in of C-rich material (not the nuclear burning)
- => Determine the radius of entropy corresponding to the runaway and mix to estimate C

Corrolar: 'Classical' overshooting is not allowed



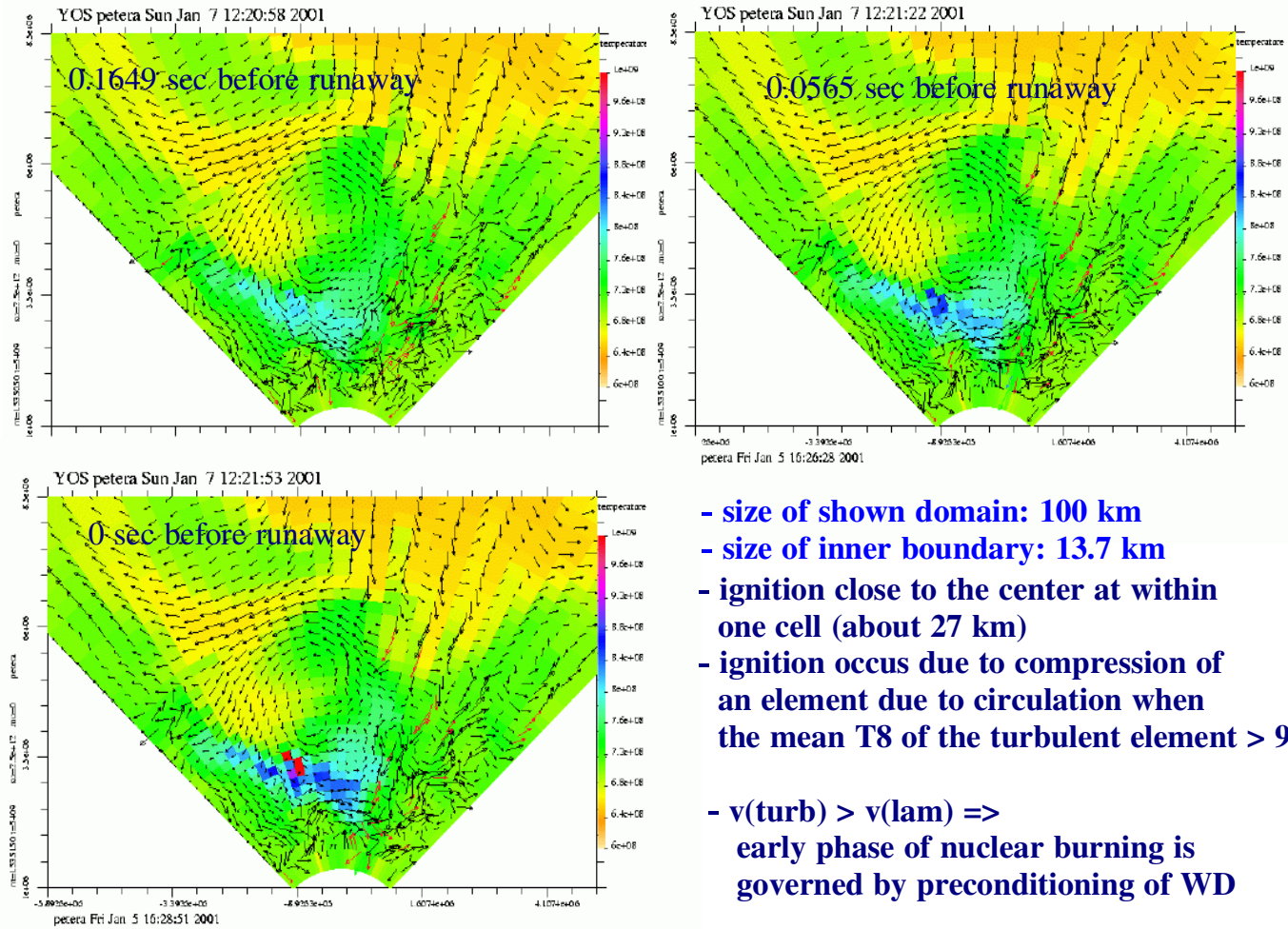
# Temperature and velocity evolution before runaway

Longest velocity vector (black,red,green) =(40/80/120 km/sec) ;  $500E8 \text{ K} < T < 1.E9 \text{ K}$



# Temperature and velocity evolution before runaway

Longest velocity vector in black = 50 km/sec ;  $600E8 \text{ K} < T < 1E9 \text{ K}$



- size of shown domain: 100 km
- size of inner boundary: 13.7 km
- ignition close to the center at within one cell (about 27 km)
- ignition occurs due to compression of an element due to circulation when the mean  $T_8$  of the turbulent element  $> 9$
- $v(\text{turb}) > v(\text{lam}) \Rightarrow$   
early phase of nuclear burning is governed by preconditioning of WD

## Some Uncertainties and Open Questions

### a) C12(alpha,gamma)O16 reaction rate

#### Influence on the ignition point:

Enhancement factor F	Change of final C-concentration	Distance of ignition
200	26 +- 1 %	90 km
50	32.5	86 km
20	35.5	71 km
4	36.2	32 km
1	37.0	27 km

=> likely, no qualitative change of the results

### b) Some limitations (just mentioned)

#### - problem of invers cascades (for incompressible fluids)

(statistically, turbulent cascade propagates towards small scales in 3-D where it decays by molecular viscosity whereas 2-D cascades go to larger scales  
=> life-times goes to infinity for 2-D for low viscosity)

This law results from quadratic invariants in mom.-energy equations

In compressible fluids, first order term do not vanish and LT become similar (MHD-turbulence, e.g. Stein & Ostriker 2001) but still ...

#### - numerical viscosity is important (limited resolution)

# Final Discussions and Conclusions

- Change of the physics of the thermonuclear runaway
  - a) classical, spherical picture of compressional heat (Sato et al. 1976)
    - > rising blobs in a static WD (Garcia & Woosley 1995)
    - > (now) importance of initial velocity field

*The explosion is determined by the preconditioning of the WD !!!*

- The chemical profile 'survives' the runaway but the central C/O increases from 23 % to 37 %
  - > energy release during the deflagration phase is modified (scale of instabilities)
  - > reduction of jump in C/O by a factor of 3 and possible effect on the DD-transition
- Ignition occurs in one confined region (no multiple spots in our example. Is this true in general?)
- Speed and structure of the deflagration front will be determined by the large scale velocity fields prior to the runaway